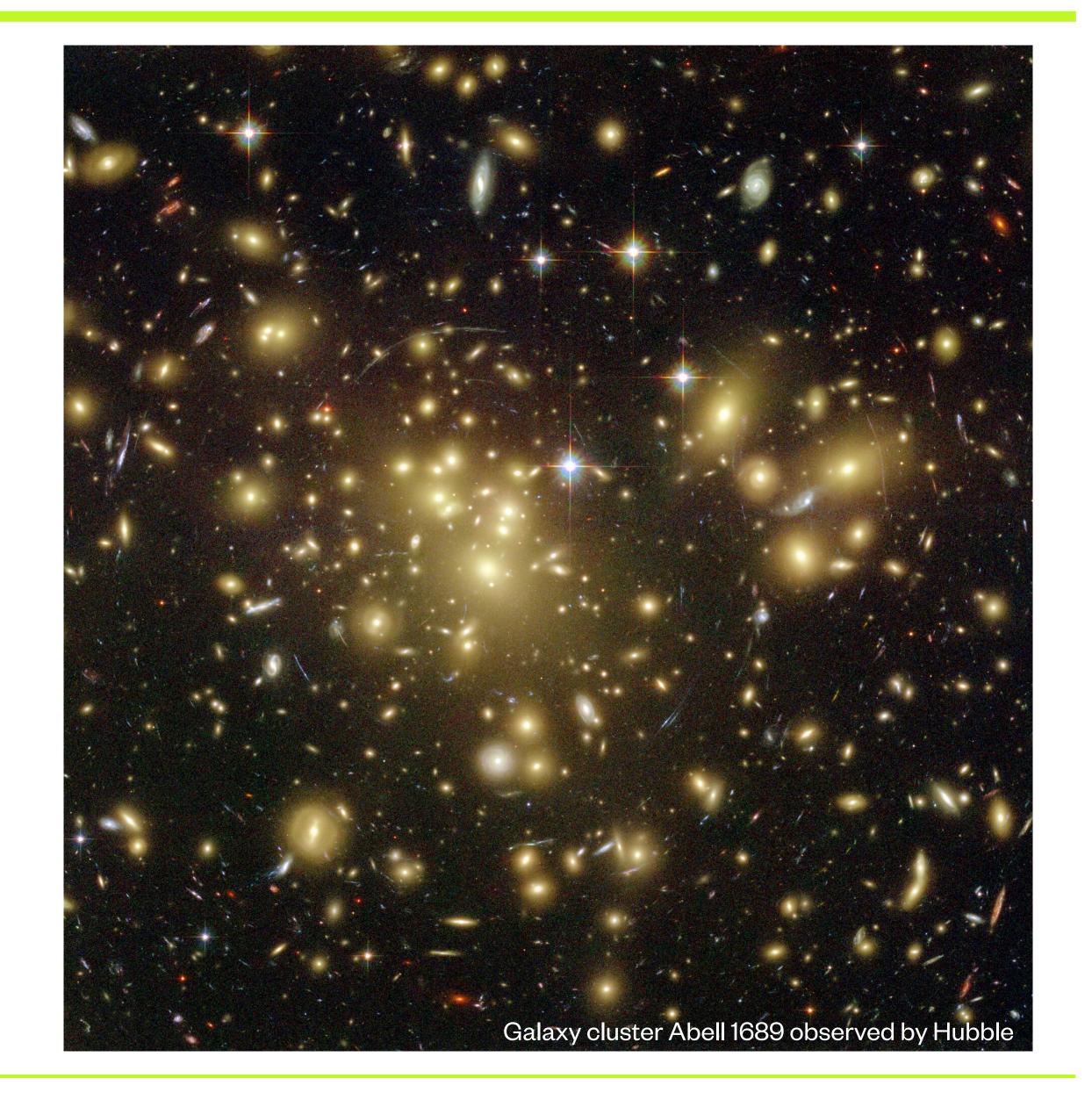
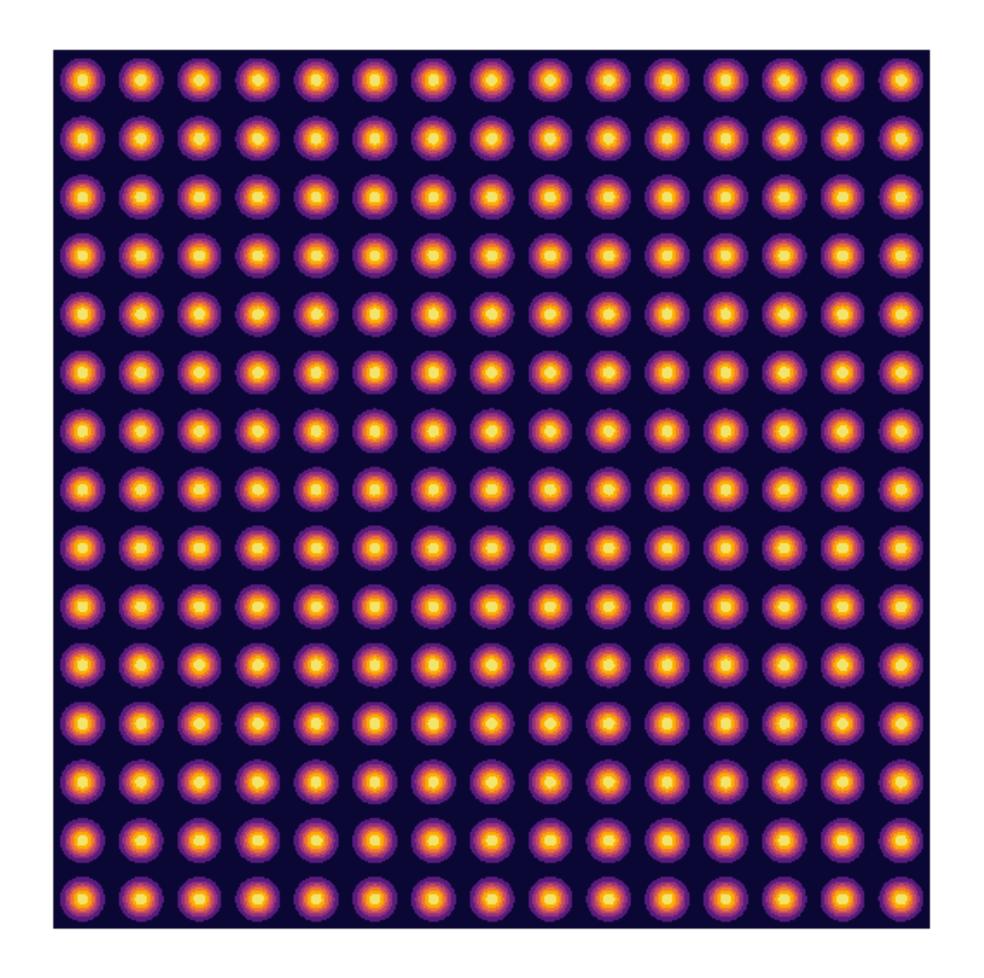


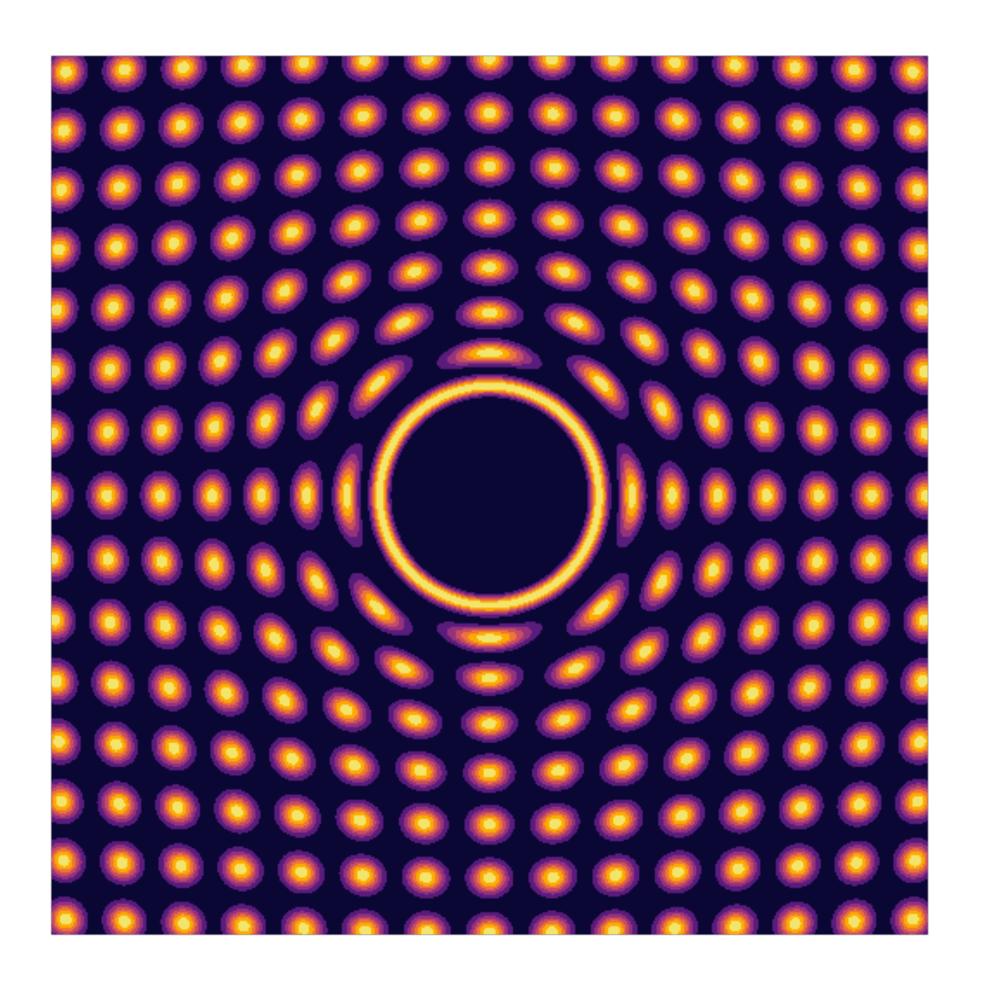
Galaxy clusters

- Largest bound objects in the universe $> 10^{14}\, \rm M_{\odot}$
- Composition
 - 85% dark matter
 - 12% hot gas
 - 3 % stellar mass
- They provide strong constraints on the matter content, geometry, the nature of gravity and the formation of structure in the universe and gravitational lensing gives information on all of this!



CALUM MURRAY 2/15



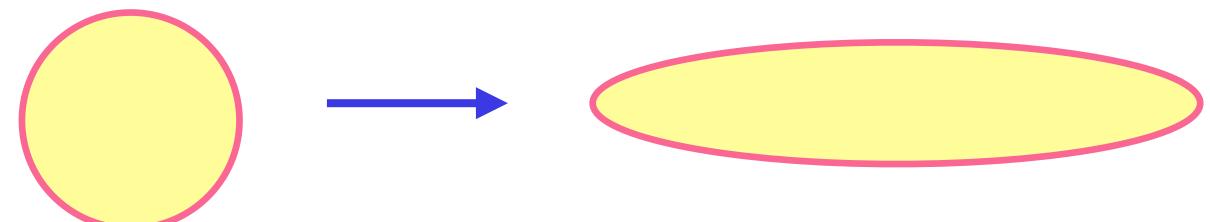


Field of **unlensed** galaxies

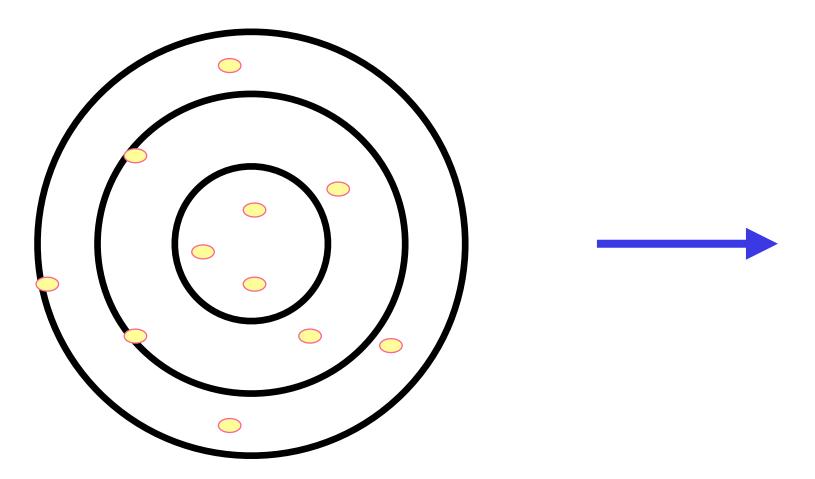
Field of **lensed** galaxies

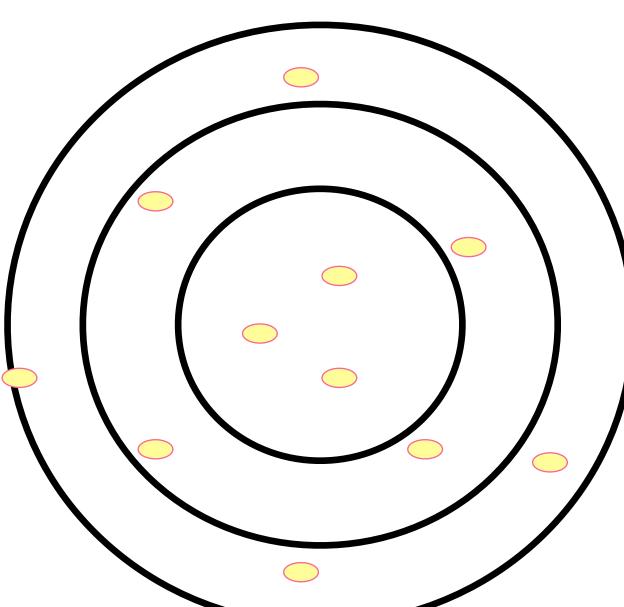
Cluster Lensing

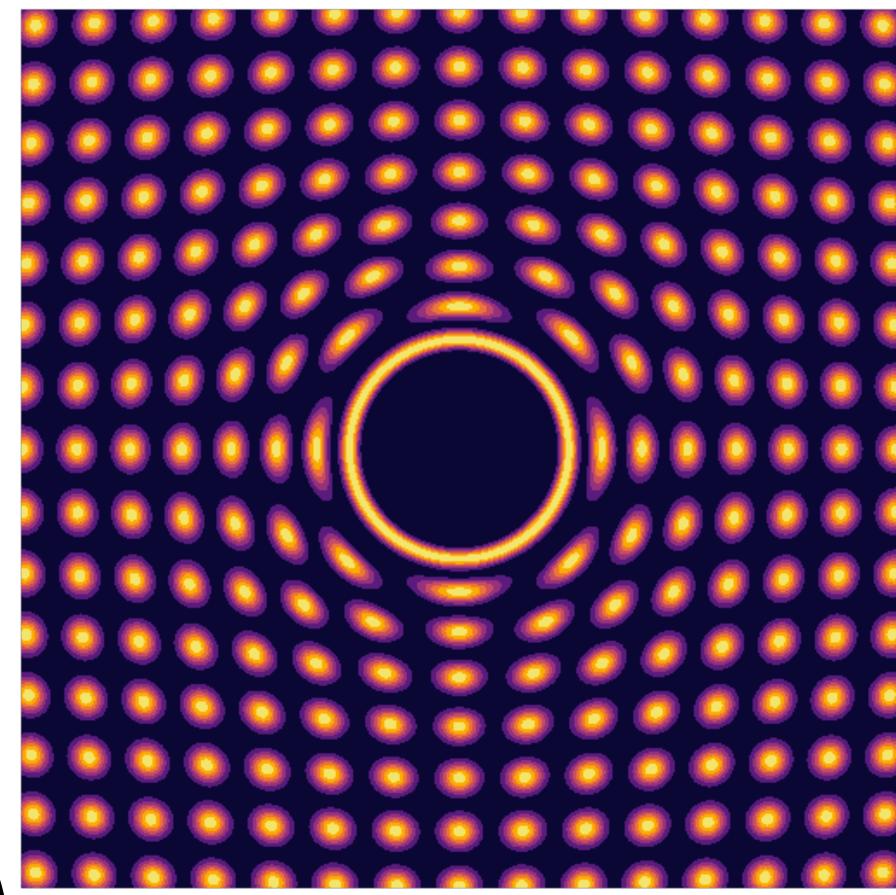
- Shears galaxy images



- Solid angles on the sky are amplified/ galaxies are deflected from the lens centre
- Galaxy magnitudes are amplified

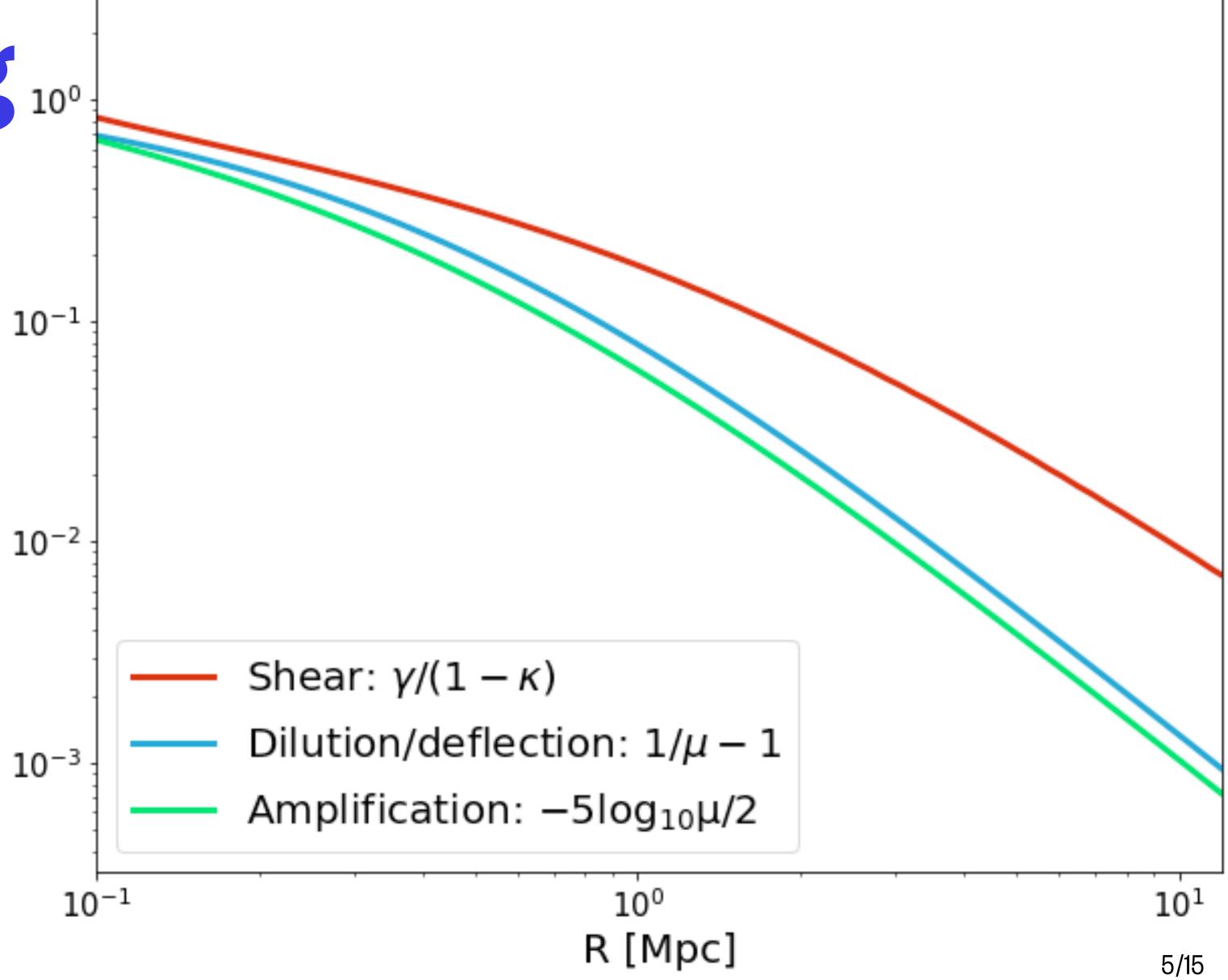






Cluster Lensing 100

- We will use the **amplification** and **dilution**!
 - Completely different
 systematics from shear,
 magnitudes opposed to shape
 measurements
 - We can go deeper in magnitude =>more galaxies



Single magnitude cut

- Count the number of galaxies
 - Galaxies are **magnified** which **introduces** faint galaxies into the sample
 - -Solid angles on the sky are magnified which reduces galaxies per solid angle

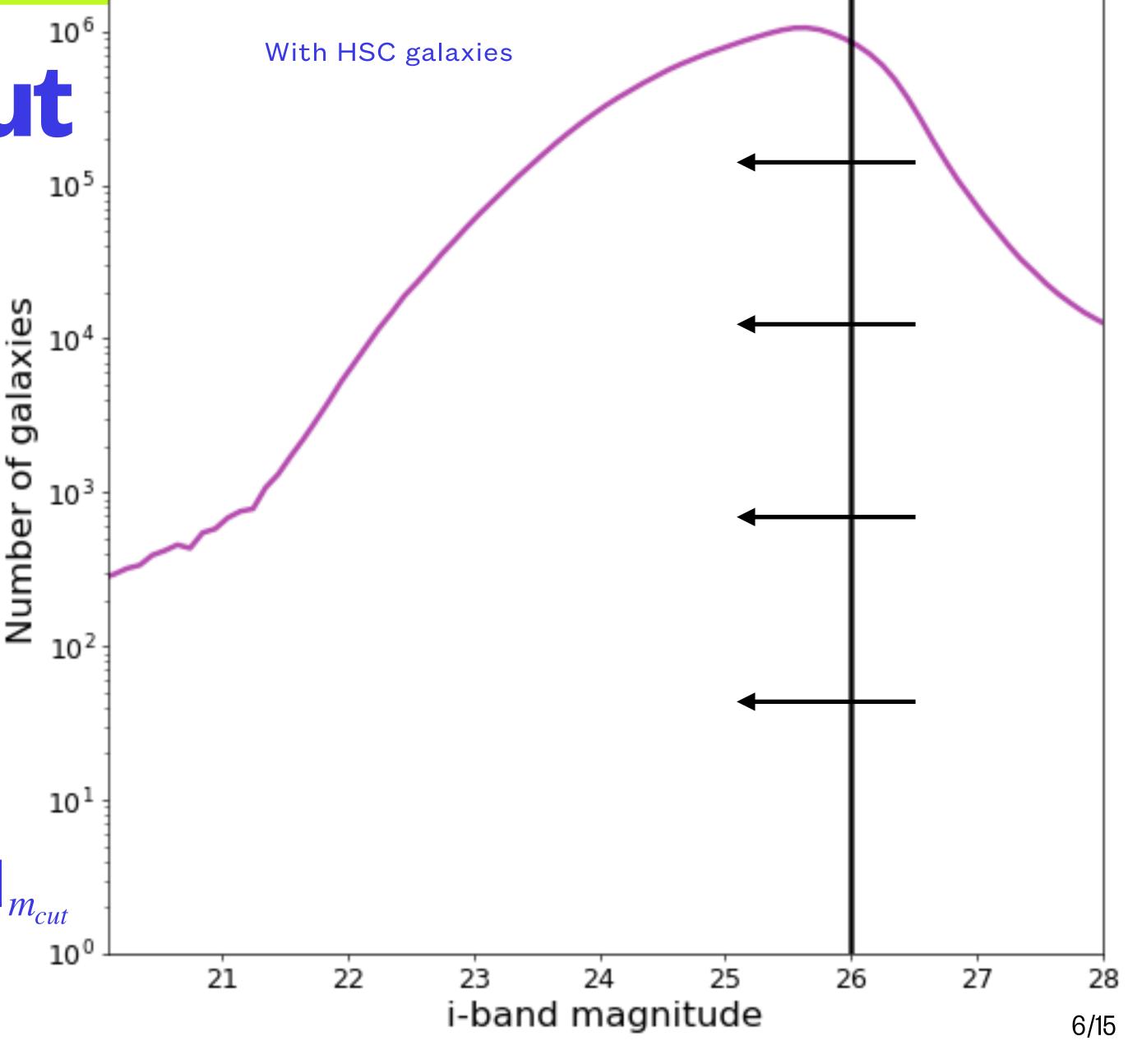
$$n_{obs}(\overrightarrow{\theta}) \approx n_o \left[1 + 2\kappa(\overrightarrow{\theta})(\alpha - 1) \right]$$

- n_o is the intrinsic galaxy distribution

- n_{obs} is the observed distribution

$$\alpha = 2.5 \frac{dlog_{10}n}{dm}$$

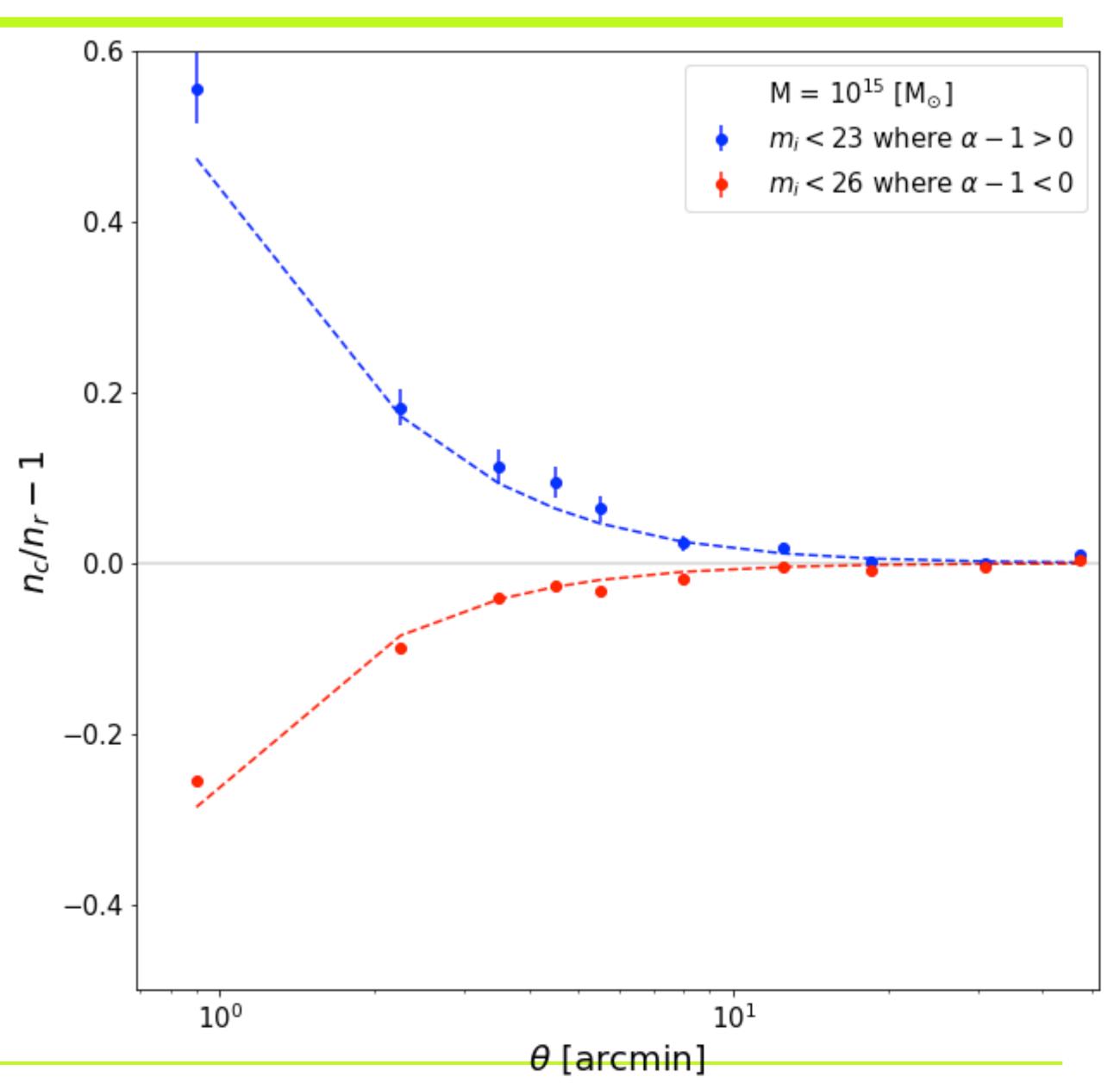
 $\bar{\kappa}$ is the lensing convergence



Single magnitude cut

- Amplification or dilution can win out \to the number of galaxies may increase or decrease depending on α
- The competition between the two effects will reduce our signal

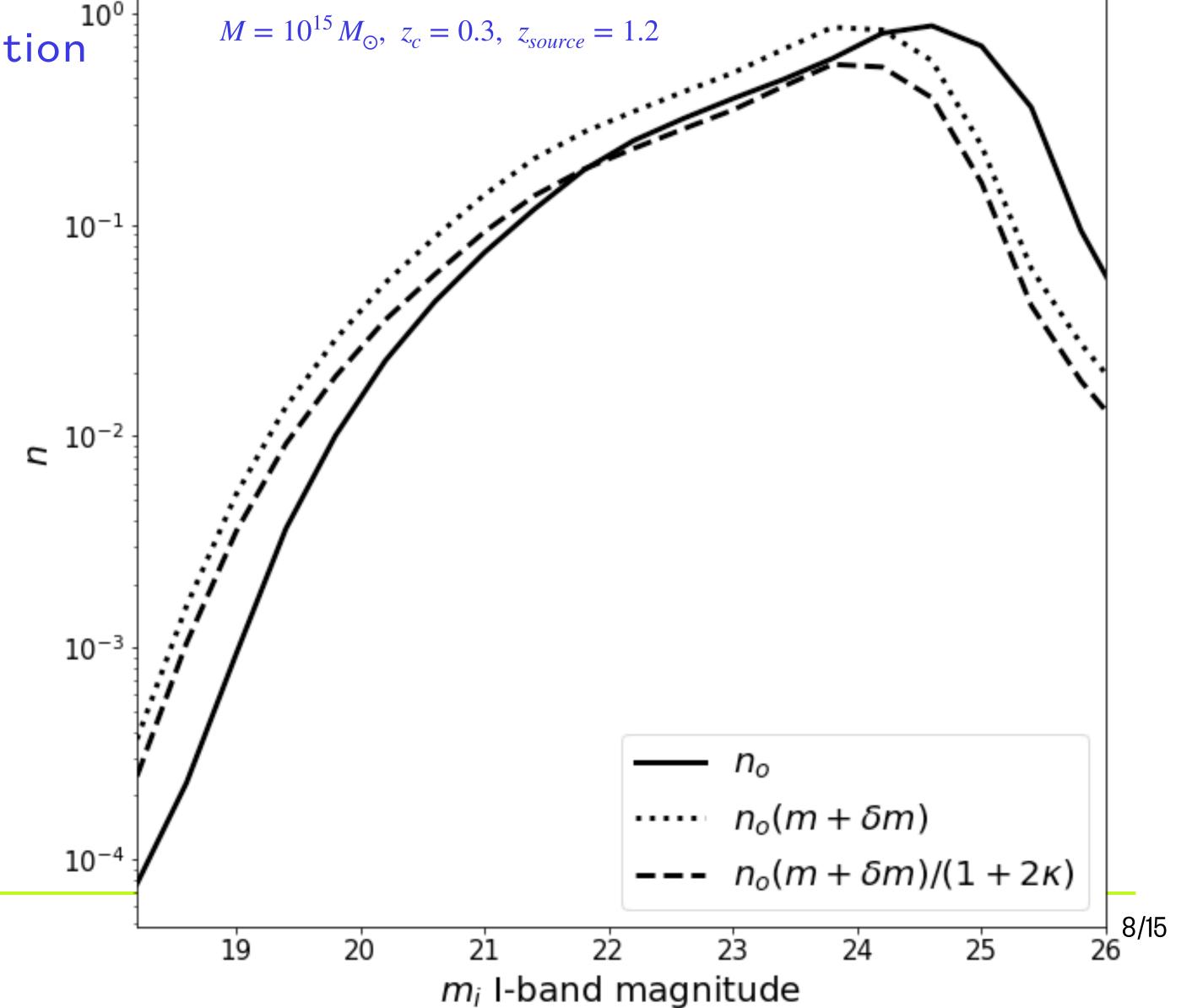
$$n_{obs}(\overrightarrow{\theta}) \approx n_o \left[1 + 2\kappa(\overrightarrow{\theta})(\alpha - 1) \right]$$



New approach - full magnitude distribution

- Resolution: full galaxy magnitude distribution
 - Change in magnitude δm -> shifts distribution
 - Change in **solid angle on the sky** $A \rightarrow$ changes normalisation
- Factor of 2 reduction on lnM errors compared to a single magnitude cut!
- -(see also Ménard and Bartelmann 2002)

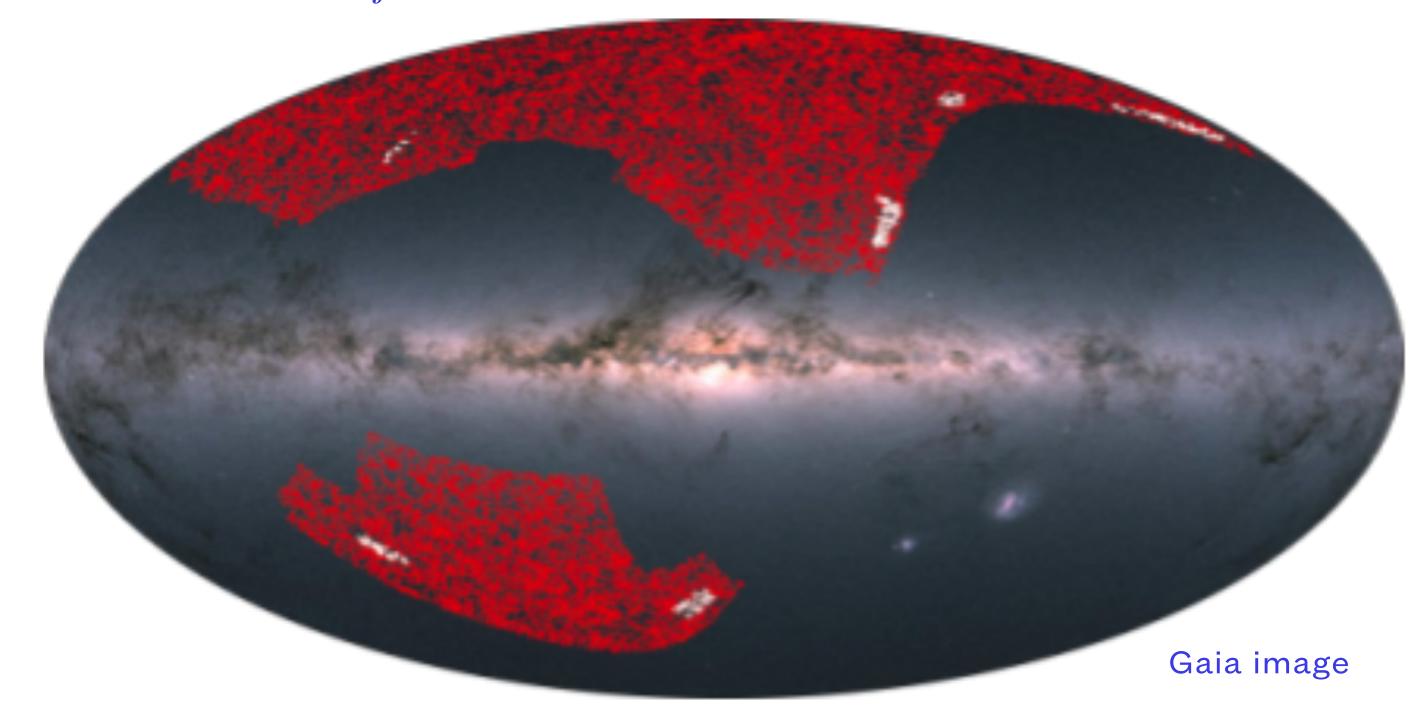
$$n_{obs} = n_o(m + \delta m)/\mu$$
$$\mu \approx 1/[(1 - \kappa)^2 - \gamma^2]$$



red MaPPer clusters

- Clusters found with redMaPPer in SDSS data
- 200 clusters with redshift > 0.3 and richness > 40
- We use Hyper Suprime Cam
 (HSC) wide field galaxies for our weak lensing data
- -Using the full likelihood we can constrain the mass

$$ln\mathcal{L} = -\frac{1}{2} \sum_{ijk} \left(n_{obs}(\theta_i, m_j, z_k) - n(\theta, m, z \mid M_{lens}) \right)^2 / \sigma_{ijk}^2$$

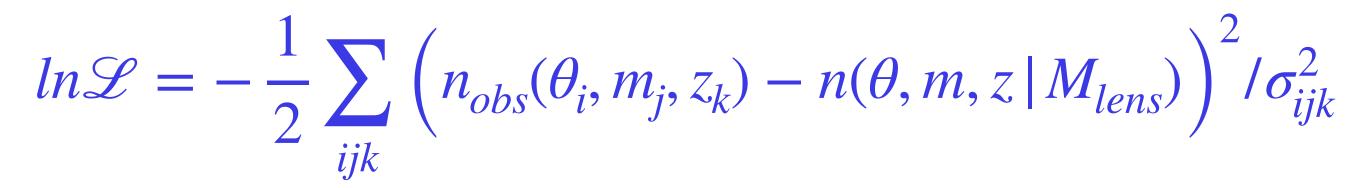


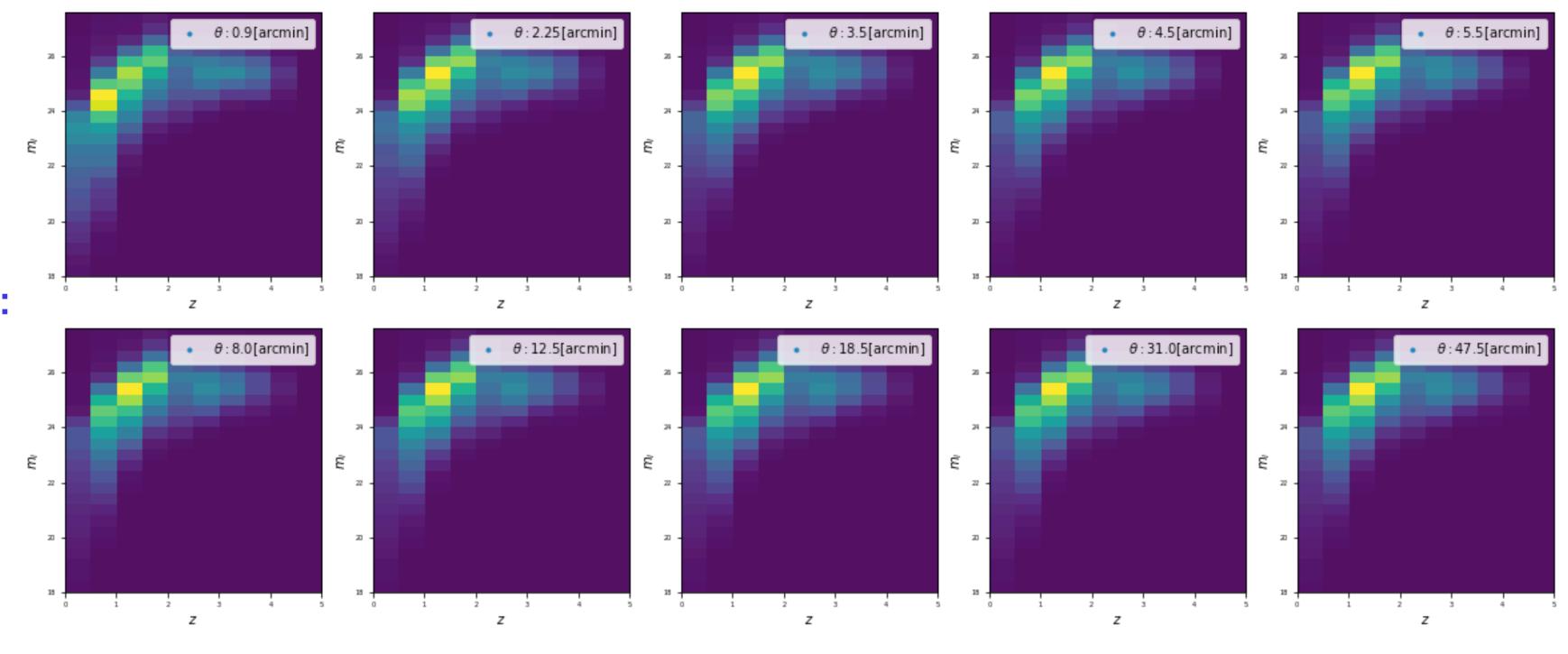
red MaPPer clusters

-Using the full likelihood we can constrain the mass using

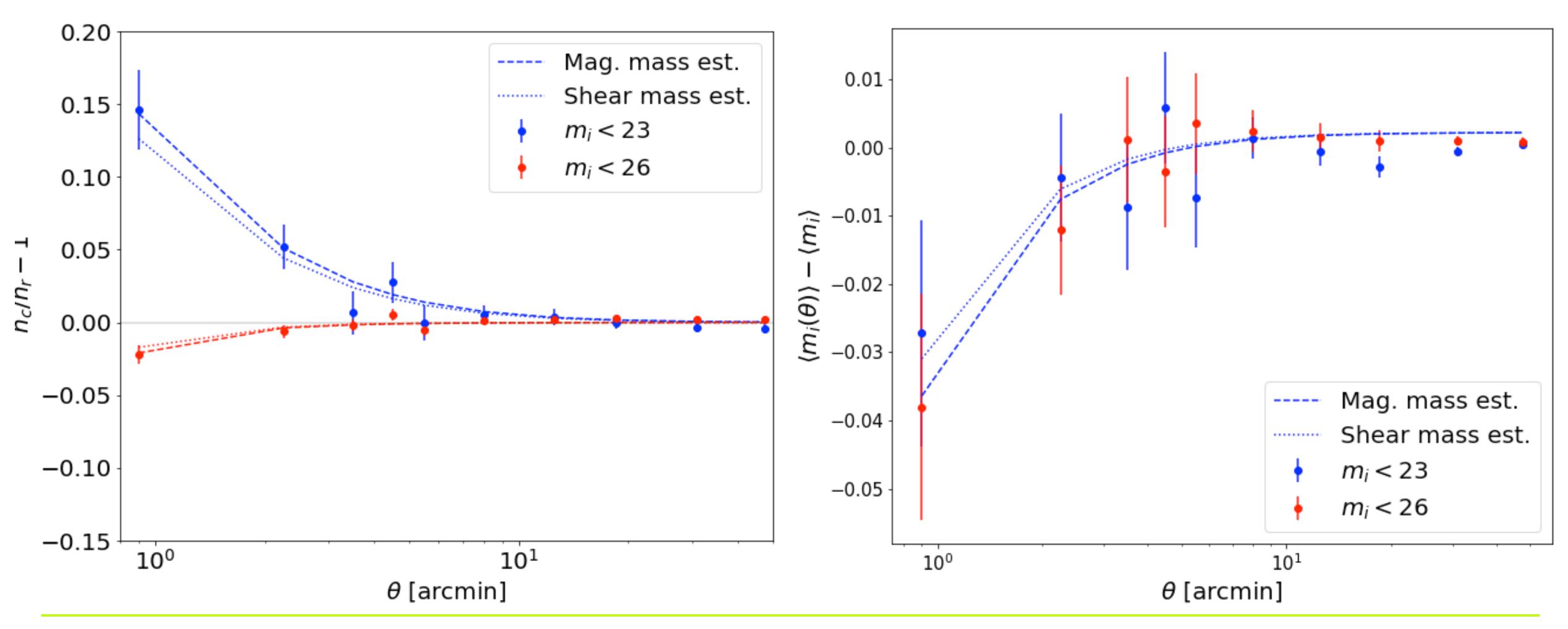
- -6 angular bins: $\theta \in [0.9,10]$ [arcmin]
- -4 bins in redshift: $z \in [1,3]$
- -14 bins in i-band magnitude: $m_i \in [20, 25.5]$

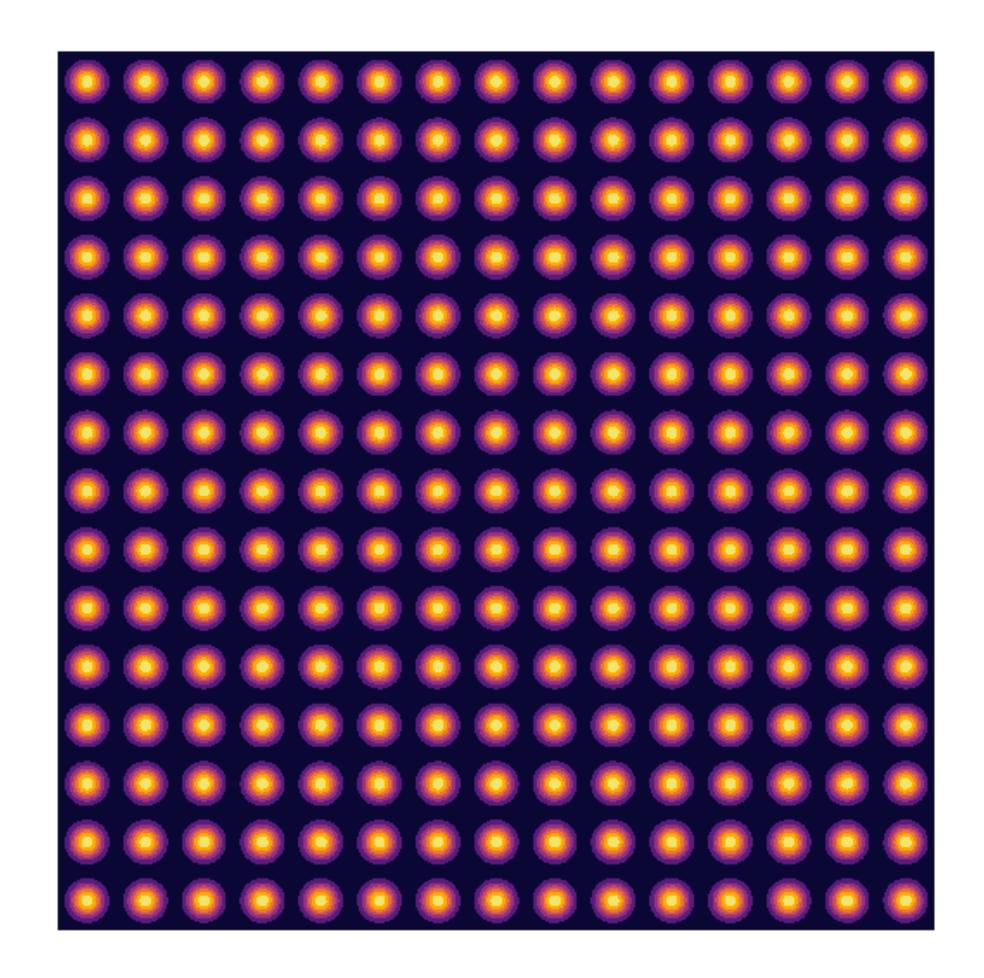
Magnitude bins





$\log_{10} M_{\text{stack}} = 14.37 \pm 0.04$





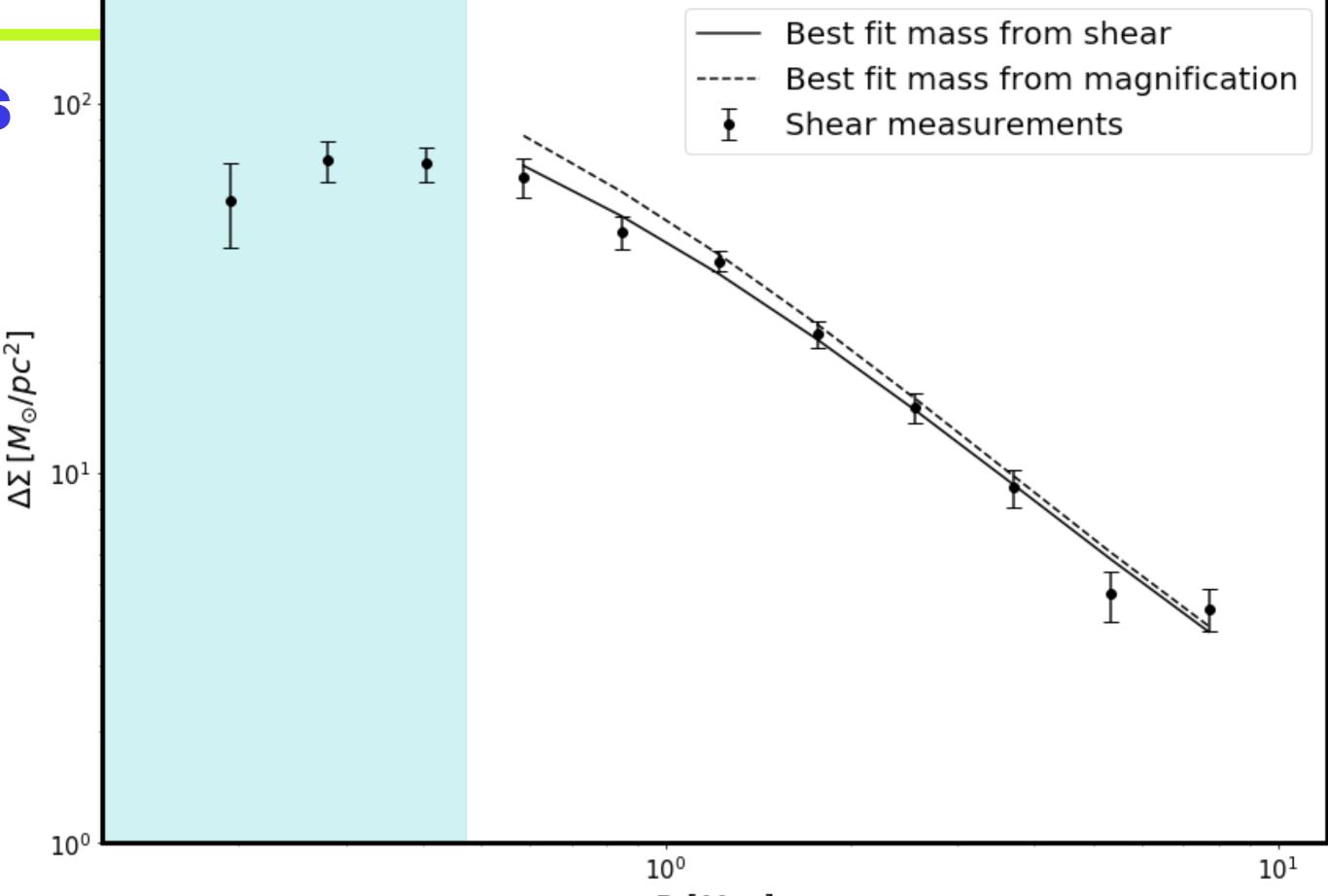
Field of **unlensed** galaxies

Field of **lensed** galaxies

Comparison to shear analysis 102

$$\epsilon_{+\text{obs}} \approx \epsilon_{+\text{int}} + \gamma$$

- We are now sensitive to the excess surface mass density (opposed to the surface mass density for magnification)
- Murray et al. 2022 Measuring weak lensing masses on individual clusters
- Consistent masses and competitive constraints

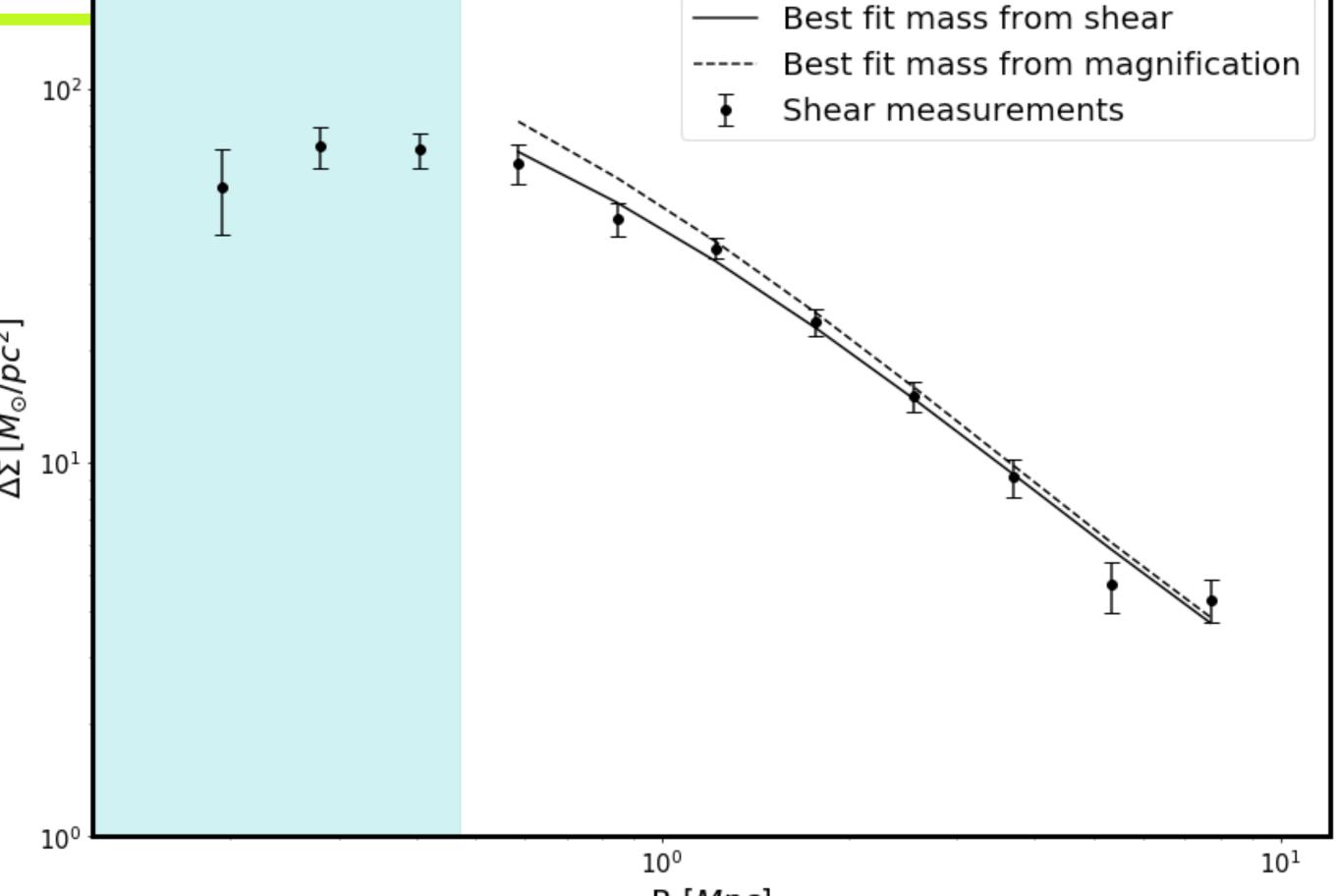


Magnification mass: $\log_{10} M_{\text{stack}} = 14.37 \pm 0.04$

Shear mass:
$$\log_{10} M_{\text{stack}} = 14.31 \pm 0.03$$

Comparison to shear analysis 102

- Consistent masses and competitive constraints
 - ~ twice as many galaxies ($m_i < 25.5$ rather than $m_i < 24.5$ for shear)
 - Combination of amplification and dilution effects
 - Magnification is less sensitive to the cluster concentration



Magnification mass: $\log_{10} M_{\text{stack}} = 14.37 \pm 0.04$

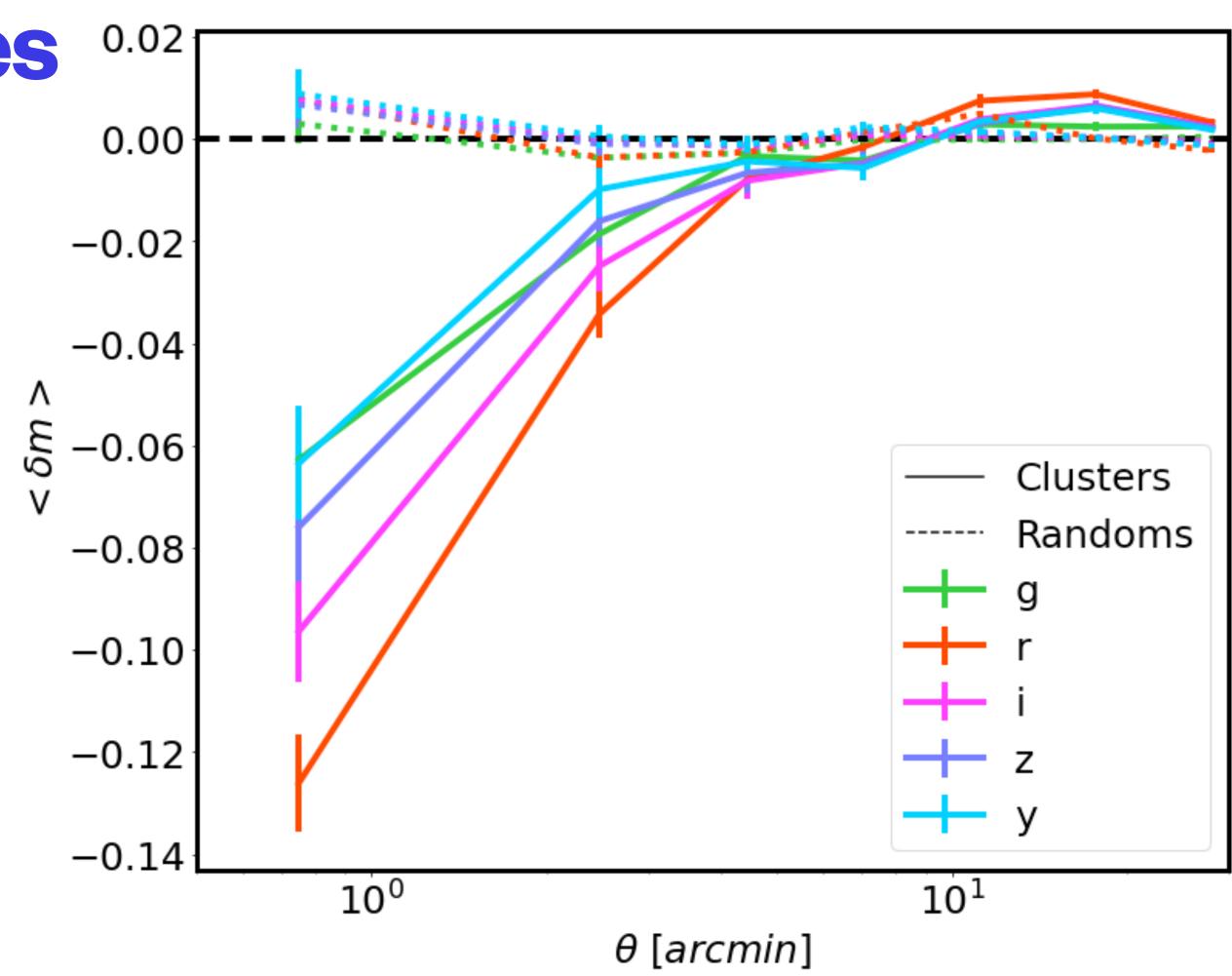
Shear mass: $\log_{10} M_{\text{stack}} = 14.31 \pm 0.03$

Stacked magnitude profiles

- Using a subsample of 90 clusters in the redshift interval $0.2 < z_{cluster} < 0.3$
- We measure the average magnitude for a stack of clusters in annuli from the cluster centre
- Clear chromatic signal
- **Attention,** lensing introduces colour changes, faint galaxies which are introduced to the sample have different colours to bright galaxies
- These profiles have been used to measure dust, not strictly true (Menard et al. 2009)

$$\langle \delta m \rangle = \langle m(\theta) \rangle - \langle m_{field} \rangle$$

$$m_{obs} \approx m_{int} - \frac{5}{2ln10} \left(2\kappa - \tau_{\lambda} \right)$$



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Conclusions

- We have introduced a new magnification method, using the full magnitude distribution for cluster mass estimation
 - A factor of ~2 improvement stacked mass errors compared to a single magnitude cut
- In agreement with shear results
- Competitive constraints with shear!